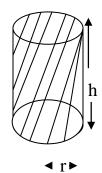
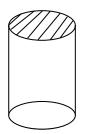
CHAPTER FOURTEEN

CYLINDERS AND CONES

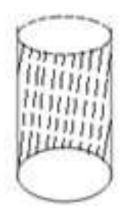
The cylinder:



- The above figure is known as a cylinder.
- The height of this cylinder is h and its radius is r.
- The shaded portion is called the total surface area of the cylinder, also referred to as the area of the cylinder.
- The area of a cylinder is made up of three parts and these are:
 - 1. The top circular flat surface area, which is also referred to as the top surface area, and which is indicated in the next diagram, by means of shading:

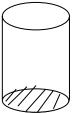


- The flat top circular surface area = πr^2 , since it is circular in shape where r = the radius.
 - 2. The curved surface area, which is indicated by means of shading, in the next figure:



- The curved surface area = $2 \pi rh$, where h = the height.

The bottom circular surface area, which is indicated in the next diagram by means of shading:

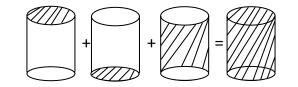


- The bottom surface area = πr^2 , since it is also circular in shape.

The area of a cylinder:

The total surface area of a cylinder is therefore had by adding together all these three surface areas,

i.e



 $\pi r^2 + \pi r^2 + 2\pi rh = 2\pi r^2 + 2\pi rh = 2\pi r(r+h).$

- Q1. The height of a cylinder is 5cm and its radius is 2cm. Calculate
 - a. its flat top circular area.
- b) its flat bottom circular area.

c) its curved surface area.

d)its total surface area. [Take $\pi = 3.14$].

Soln.

h = 5cm, r = 2cm and π = 3.14.

- a. The flat top surface area = $\pi r^2 = 3.14 \times 2^2 = 3.14 \times 4 = 12.56 cm^2$
- b. The flat bottom surface area = $\pi r^2 = 3.14 \times 2^2 = 3.14 \times 4 = 12.56 cm^2$
- c. The curved surface area = $2\pi rh = 2 \times 3.14 \times 2 \times 5 = 62.8 cm^2$
- d. The total surface area = top surface area + bottom surface area + curved surface area = $12.56cm^2 + 12.56cm^2 + 62.8cm^2 = 87.9cm^2$.

N/B: Also the total surface area = $2 \pi r(r + h) = 2 \times 3.14 \times 2(2 + 5) = 12.56(7)$ = 87.9cm².

Q2. A cylinder has a height of 40m and a diameter of 12m. Determine

- a. its bottom circular area .
- b. its curved surface area.
- c. Its total surface area. [Take $\pi = 3.142$]

Soln:

Since d =12m \Rightarrow $r = \frac{12}{2} = 6m$. Also $\pi = 3.142$ and h = 40m.

- a. The bottom circular surface area = πr^2 = 3.142 \times 6^2 = 3.142 \times 36 = $113m^2$
- b. The curved surface area = $2\pi rh = 2 \times 3.142 \times 6 \times 40 = 1508m^2$
- c. The total surface area = $2\pi r(r + h) = 2 \times 3.142 \times 6(6 + 40) = 1734 \text{m}^2$.

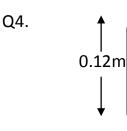
Q3. A water storage tank is to be constructed using aluminum. If it is to have a diameter of 40m and a height of 120m, determine the amount of aluminum that will be needed to construct

- a. its curved surface area.
- b. the whole tank. [Take π or pie = 3.14].

Soln.

Since d = 40m \implies $r = \frac{40}{2} = 20m$. Also pie = 3.14 and h = 120m.

- a. The amount of aluminum which is needed to construct the curved surface area = the curved surface area = $2\pi rh = 2 \times 3.14 \times 20 \times 120 = 15072m^2$
- b. The amount of aluminum needed to construct the whole tank = the total surface area = $2\pi r(r + h) = 2 \times 3.14 \times 20(20 + 120)$ = $126(140) = 17640m^2$



The given figure is that of a drinking cup, which is to be constructed using plastic. If it is to be 0.12m long and have a diameter of 8cm, determine the quantity of plastic needed for its construction. [Take $\pi = 3.142$].

N/B:

- A drinking cup has no top surface area $\Rightarrow plastic$ will only be needed to construct the curved surface area and the bottom surface area.
- Also since the height is given in metres and the diameter in centimetres, the metres must be converted into centimetres.

Soln.

h = 0.12m = 0.12 x 100 = 12cm.

8cm

 $\mathsf{D} = 8\mathsf{cm} \Longrightarrow r = 4cm.$

The amount of plastic needed to construct the curve surface area = $2\pi rh = 2 \times 3.142 \times 4 \times 12 = 302 cm^2$.

The amount of plastic needed to construct the bottom surface area = bottom surface area = $\pi r^2 = 3.142 \times 4^2 = 3.142 \times 16 = 50 cm^2$.

The quantity of plastic needed to construct the cup = amount of plastic needed to construct the curved portion + the amount of plastic needed to construct the bottom surface = $302 + 50 = 352cm^2$.

Q5. The curved surface area of a cylinder of height 80cm is $2880cm^2$. Calculate

- i. Its total surface area .
- ii. Its circular top surface area. [Take $\pi = 3.14$]

Soln.

The curved surface area = $2\pi rh$, and since the curved surface area of the cylinder is given as $2880cm^2 \Rightarrow 2\pi rh = 2880$, $\Rightarrow 2 \times 3.14 \times r \times 80 = 2880$,

$$\Rightarrow 502r = 2880, \Rightarrow r = \frac{2880}{502} \Rightarrow r = 5.7cm.$$

- i. The total surface area = $2\pi r(r+h) = 2 \times 3.14 \times 5.7(5.7+80) = 36(85.7) = 3085cm^2$
- ii. The top circular surface area = $\pi r^2 = 3.14 \times 5.7^2 = 102 cm^2$.

N/B: Since in the question the heights as well as the curved surface areas were given, we must first determine the radius.

In the next question, the curved surface area is given as well as the radius. We
must therefore first determine the height.

Q6. The curved surface area of a cylinder whose radius is 5cm is $628cm^2$. Determine its total surface area.

Soln.

r = 5cm and h = ?

Since the curved surface area = $628 cm^2$, then $2\pi rh = 628 \implies 2 \times 3.14 \times 5 \times h = 628, \implies 31.4h = 628 \implies h = \frac{628}{3.14} = 20.$

Total surface area = $2\pi r(r+h) = 2 \times 3.14 \times 5(5+20) = 31.4(25) = 785cm^2$

Q7. A cylinder has a top surface area of 12.56cm² and a height of 0.8m. Calculate

- a. its curved surface area.
- b. its total surface area. [Take $\pi = 3.142$]

Soln.

Top surface area = 12.56 cm², h = 0.8m = 0.8m x 100 = 80 cm.

$$\pi = 3.142 \text{ and } r = ?$$

The top surface area is given by πr^2 , and since this = 12.56cm², then

$$\pi r^2 = 12.56, \Longrightarrow r^2 = \frac{12.56}{3.142} = 4.$$

Since $r^2 = 4 \Rightarrow r = \sqrt{4} = 2$.

- a. Curved surface area = $2\pi rh = 2 \times 3.142 \times 2 \times 80 = 1005 cm^2$
- b. The total surface area = $2\pi r(r + h) = 2 \times 3.142 \times 2(2 + 80) = 12.56(82) = 1030 cm^2$.

The volume of cylinder:

- The volume of a cylinder is the amount of gas, liquid or solid which it can contain or hold.
- The volume of a cylinder is given by $v = \pi r^2 h$, where r = the radius and h = the height.

Q1. A cylinder has a height of 80cm and a diameter of 20cm. Calculate

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a. its volume
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b. the volume of air it will contain when it is

i. full ii. half full.

[Take $\pi = 3.143$]

Soln.

 $d = 20 \text{cm} \Rightarrow r = 10 \text{cm}.$

- a. Volume = $\pi r^2 h = 3.14 \times 10^2 \times 80 = 25120 cm^3$.
- b. i. The volume of air it will contain when it is full = $25120 cm^3$.

ii. The volume of air it will contain when it is half full = $\frac{1}{2} \times 25120 = 12560 cm^2$.

Q2. A cylinder is to be constructed in order to have a volume of 5540cm³. If it is to have a radius is 20cm, calculate its height.

Soln.

$$v = 5540 cm^3$$
, $r = 20 cm$ and $h = ?$

Since $v = \pi r^2 h$, then 5540 = 3.14× 20² × h, \Rightarrow 5540 = 1256h \Rightarrow $h = \frac{5540}{1256} = 4.4$,

 \therefore the height = 4.4cm

Q3. A cylindrically shaped water tank, can hold 7000cm³ of water when it is full. If it has a height of 50cm, determine its radius.

Soln.

 $v = 7000cm^3$, h = 50cm and r = ?

Since $v = \pi r^2 h$, then 7000 = 3.14 × r^2 × 50, \Rightarrow 7000 = 157 r^2 , \Rightarrow $r^2 = \frac{7000}{157}$, \Rightarrow $r^2 = 44.5$, \Rightarrow $r = \sqrt{44.5} =>$ r = 6.6cm